

Physiological Closed-loop Controllers for MDCPS

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Model-Driven Safety Analysis of Closed-Loop Medical Systems

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Overview

1. Medical Case Study
2. Modeling and analysis
 1. Matlab Model
 2. Uppaal Model
3. Discussion

Interoperability for Patient Safety

- Modern medical care is heavily reliant on devices
 - Sensors: patient monitors, thermometers, glucose meters, EKG
 - Actuators: infusion pumps, radiation therapy, pacemakers
- Caregiver is always in the loop
 - Continuous monitoring is not possible
 - Relies on alarms to detect events
- Alarms are frequently irrelevant (false positive) or ignored (alarm fatigue)

PCA Case Study

- Patient Controlled Analgesia
 - Common technique for delivering pain medication
- 1. Patient presses a button to request a dose
- 2. Overdoses result in respiratory distress, ultimately death
- 3. Pumps have safeguards, but overdoses can still happen
- 4. PCA is a significant source of adverse events

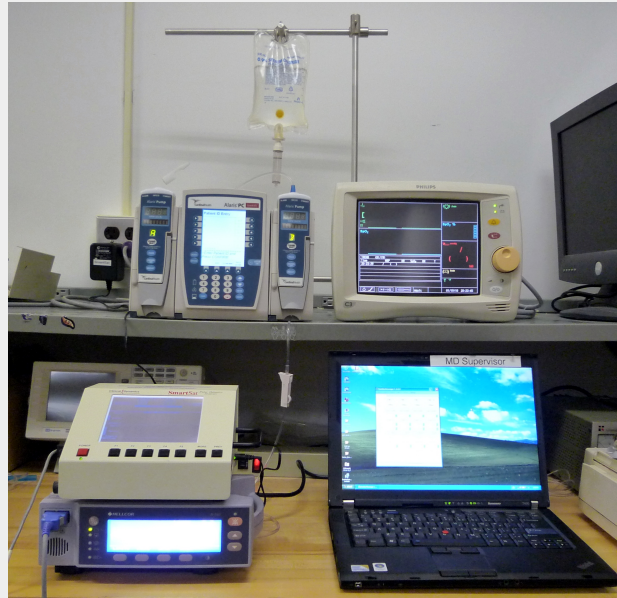


Challenges

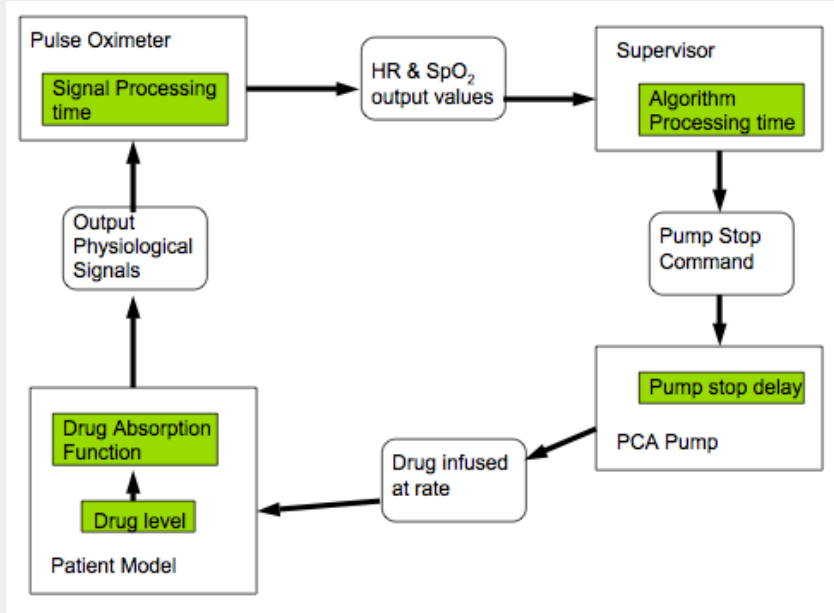
- Physical connectivity and communication infrastructure
- Patient Modeling
 - People are unpredictable
 - Models do not exist or are too complex
 - Under-actuated system with limited observability
- Verifying Safety Properties
 - Individual devices and whole system
- Regulatory Challenges
 - Who is the manufacturer of the composed system?

Case Study Components

- PCA infusion pump
- Pulse-Oximeter
- Supervisor
- Patient Model

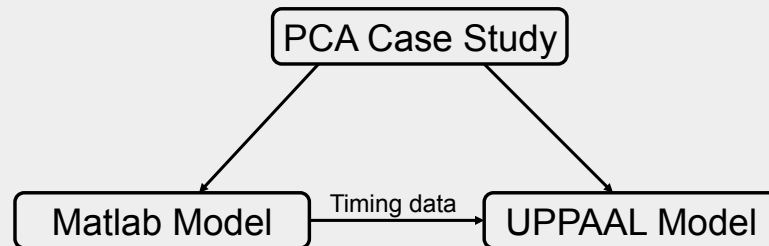


Control Loop



Modeling approach

- Matlab / Simulink model captures continuous dynamics
- Simulation provides timing data to tune the more abstract UPPAAL model
- Formal verification in UPPAAL

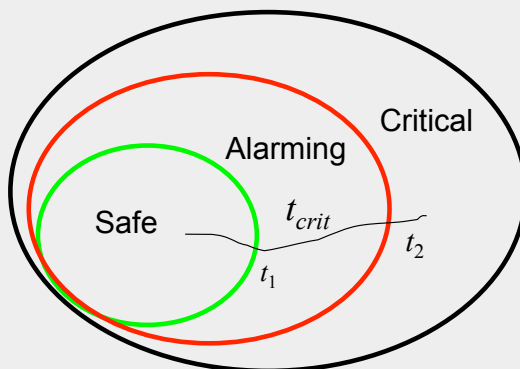


Patient Model

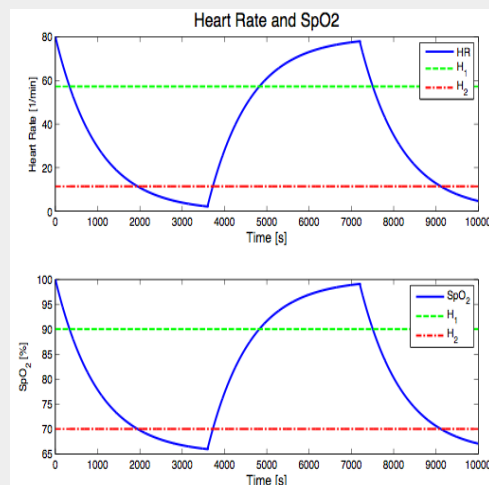
First-order continuous system

$$SpO_2 = C_{\min} + Ae^{-ct}$$

Patient Critical Regions

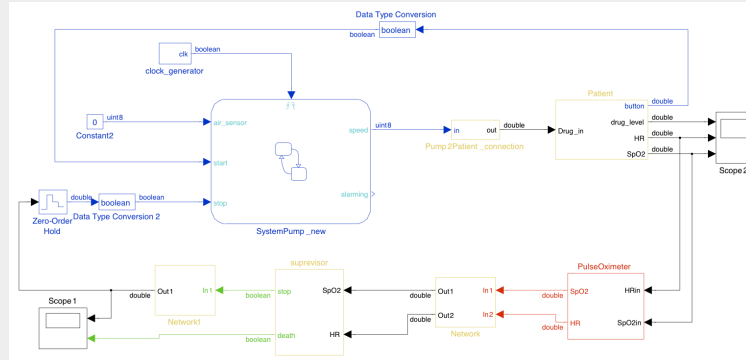


Patient Response to Drug



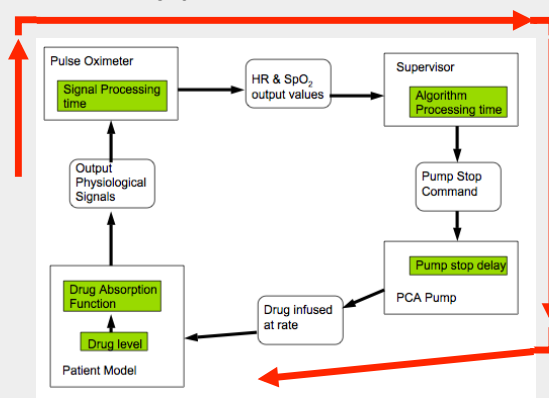
Matlab Model

- Captures the dynamics of the PCA pump, pulse oximeter, patient model, and supervisor
- Defines safe, critical, and alarming regions
- Simulations of the model allow us to estimate t_{crit}
- Allows us to study effects of faults



Key Safety Property

Pump stops in time if **total delay** $\leq t_{crit}$



Total delay is the sum of:

t_{POdel} : worst case delay from PO (1s)

t_{net} : worst case delay from network (0.5s)

t_{Sup} : worst case delay from Supervisor (0.2s)

t_{Pump} : worst case delay from pump (0.1s)

t_{P2PO} : worst case latency for pump to stop (2s)

t_{pi} : worst case patient inertia- time for drug to affect the patient (10s)

t_{crit} : shortest time the patient can spend in the alarming region before going critical

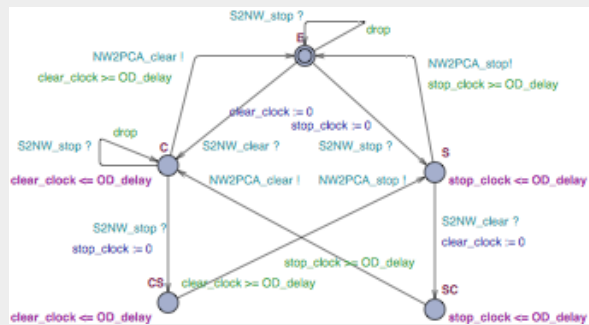
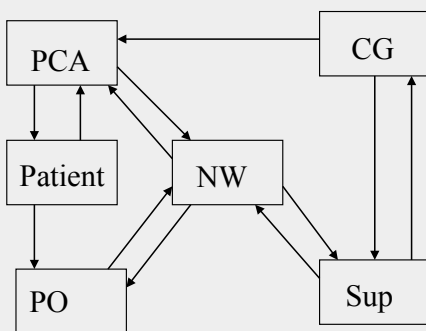
Obtaining t_{crit}

- For our patient model, determine t_{crit} analytically

$$t_{crit} = \frac{1}{\alpha} \log \frac{H_1 - C_{min}}{H_2 - C_{min}}$$

- In a more complex case, obtain through Matlab simulation
- For a more precise result, a modal value can be derived
 - E.g., account for patient context such as weight.

UPPAAL Model

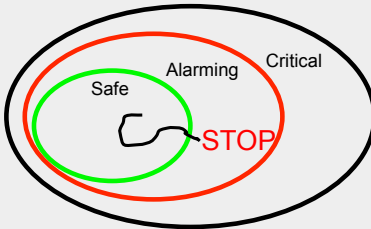
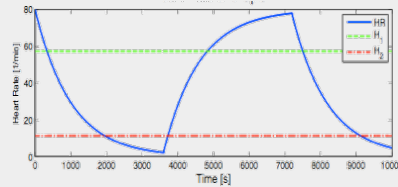


Network Component

Properties verified with UPPAAL

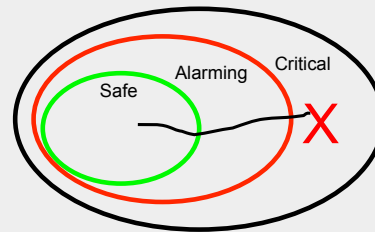
- Once SpO2 drops below pain threshold, it eventually goes back up

$A[]$ (samplebuffer < pain_thresh \rightarrow A \leftrightarrow samplebuffer \geq pain_thresh)



- The pump is stopped if patient enters alarming
 $A[]$ (samplebuffer < alarm_thresh \rightarrow A \leftrightarrow (PCA.Rstopped \vee PCA.Bstopped)

- The patient can not go into the critical region
 $A[]$ (samplebuffer \geq critical)



Effects of unreliable network

- Problem:
 - The pump may not receive stop commands.
- Solution:
 - Instead of sending simple start and stop commands, send a command giving the pump permission to run for a certain period of time.
- Open-loop stability
 - We need to determine how long the pump can run without endangering the patient

System Implementation

- FPGA boards for the device interfaces and real-time network
- Real devices where possible
- Homegrown pump prototype for control



Conclusions

- Medical CPS offer plenty of challenging problems that urgently need solutions
- Not all of these problems are technical
 - Some are organizational, cultural, etc.
- We presented first step
 - Case study of a real clinical problem
 - Modeling approach combines simulation and formal verification
- But much research is still needed

Future work

- Better patient model
 - More realistic dynamics, parametric variability
 - More sophisticated control-theoretic analysis
- Sensor fusion
 - Better reliability
 - Faster detection
- Safety in dynamically created scenarios
 - Compositional reasoning?
 - Safety case construction
- Modeling of clinical scenarios
 - Workflows, requirements for devices, safety criteria



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Current and Future Research

Closed-loop Glucose Control Systems

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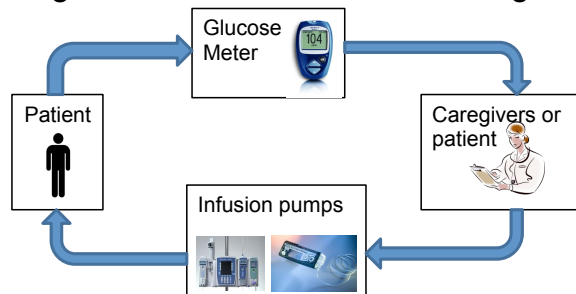


Outline

- Introduction
- Our vision
- Current state of affairs
- Our Approaches
 - Model-based safe adaptive/robust control
 - Simulation/testing based verification

Introduction

- Diabetes: a growing problem
 - **26 million (8.3% of the population) in US** have diabetes
 - 7-th leading cause of death
 - Costs \$174 billion annually
 - 5-10% are Type 1 (T1D), others are Type 2 (T2D)
- Improved blood glucose regulation benefits
 - maintain glucose level within certain ranges

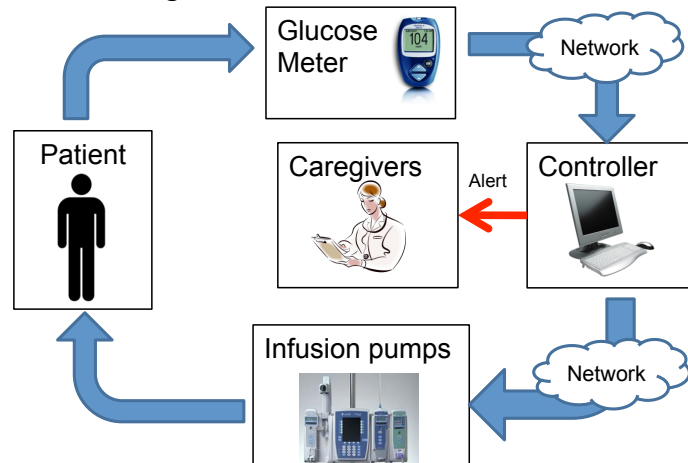


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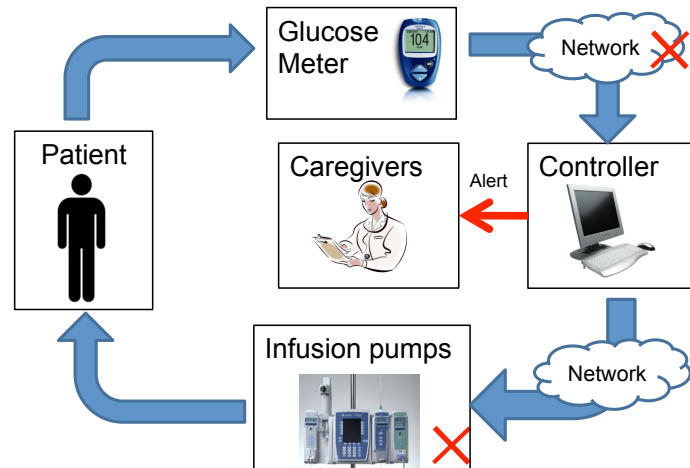
Our Vision

- A networked glucose control system
 - promote the quality of glucose regulation
 - reduce caregivers' workload, improve patient safety
- Only alert caregivers to adverse events



Research Objective (1)

- **Safe** and **effective** networked glucose control system
 - Hazards: *communication* and *components* may fail
 - How to guarantee safety under failure conditions



Research Objective (2)

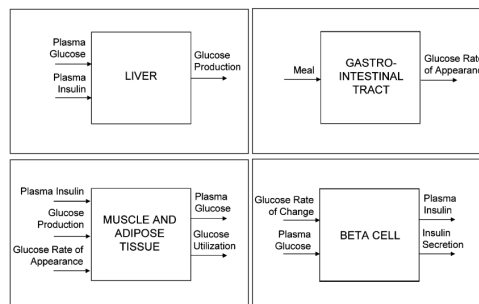
- Model-based development
 - Needs patient model and controller model
- Safety property: patient's physiological states never become critical, e.g., hypoglycemia
 - assuming all components work as assumed
 - In present of hazardous situations and uncertainties in environment, e.g., component failures, delay food feedings
- Validation and verification

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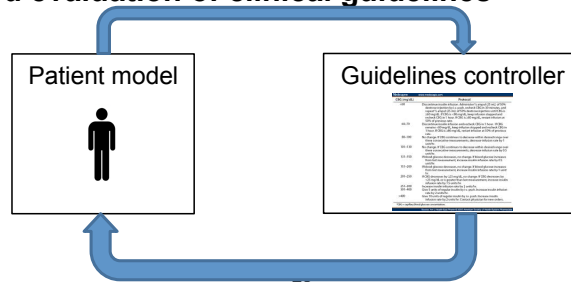
Patient Model

- Modeling the human glucose-insulin dynamics
 - 60's: simplest linear model by Bolie
 - 70's – 80's: minimal (coarse-grain) modeling strategy
 - 90's – now: maximal (fine-grain) models
 - High-order nonlinear model with many **unknown parameters**
 - Not easily identifiable
 - Man et al., 2007, meal simulation model



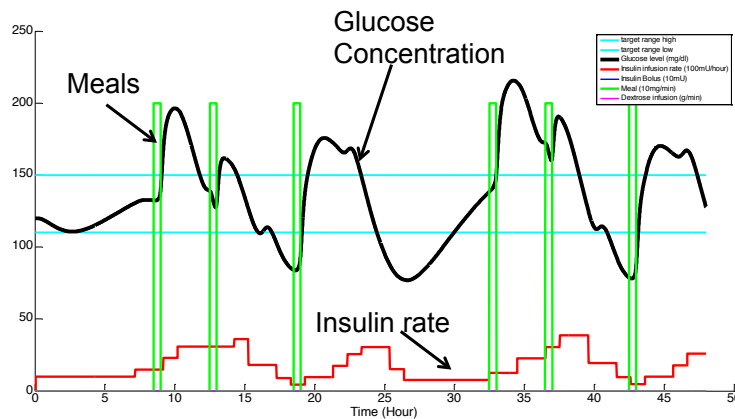
Guideline-based Controller (1)

- **Controller: clinical guidelines**
 - 5 ICU insulin infusion guidelines from a hospital
 - programmed as rule-based controllers
- **Patient model:UVa/Padova T1DM Metabolic Simulator***
 - Based on a maximal model (Man et al., 2007)
 - 30 “virtual” subjects settings
 - Full version (with 300 virtual subjects) approved by FDA in 2008 to substitute animal trials in the pre-clinical testing of certain control strategies
- **Model-based evaluation of clinical guidelines**



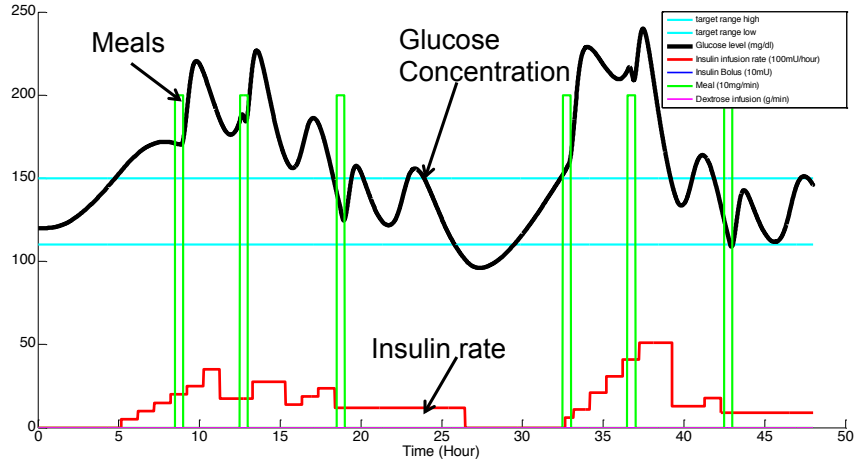
Guideline-based Controller (2)

- Guideline controls are not always effective
- Hypoglycemia (low glucose) and serious oscillations in glucose level observed on some virtual subjects
 - Example:



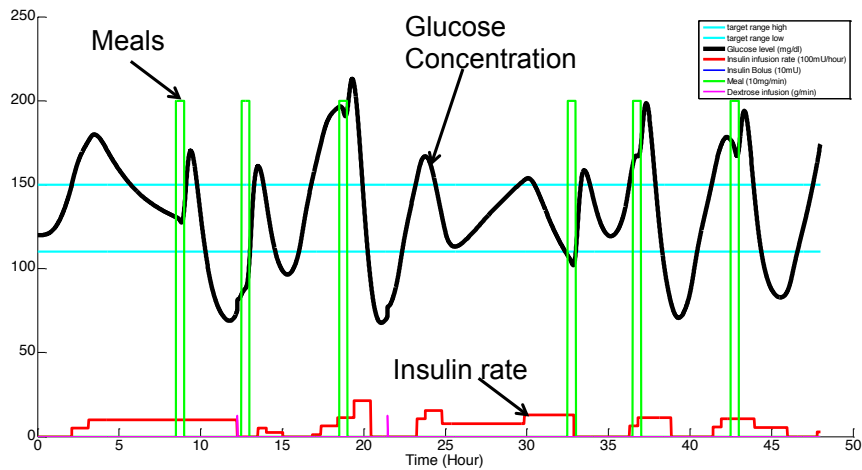
Guideline-based Controller (3)

Some subjects are more resistant to insulin



Guideline-based Controller (4)

Some subjects are sensitive to insulin



Guideline-based Controller (5)

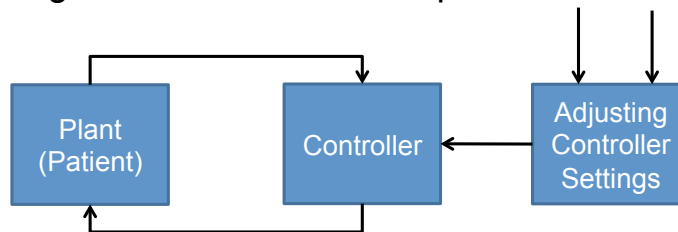
- Clinical guidelines use fixed rule tables
 - Not adaptive to inter-subject variability within the same patient population
- Need more effective controllers for the networked control system

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Adaptive/Robust Control

- Deal with physiological parameter uncertainties
 - *Adaptive approach:*
 - Adjusting controller settings at run-time
 - Explicit adaptive control: learn model parameters at run-time
 - Difficult for a ~20-D non-linear model with ~30 parameters
 - Implicit adaptive control may apply
 - *Robust approach:*
 - stabilize the plant with bounded parameter uncertainties
- Challenges: **verification** of adaptive/robust controller



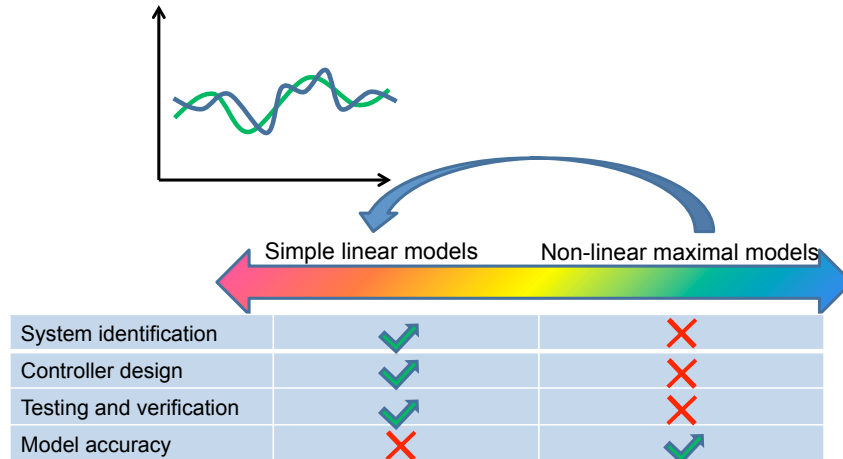
Safe Adaptive Exploration

- Adaptive control often involves learning the parameters by feeding in extreme inputs
 - Example: aggressively turning a car
- Not safe for patient-in-the-loop systems
- Open issue: adaptive exploration with safety constraints



Safe Non-linear Model Reduction

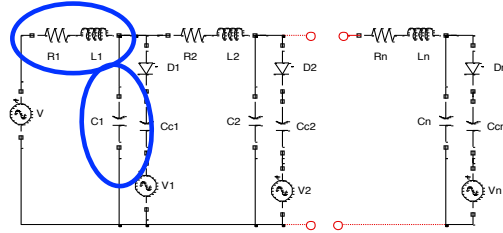
- Model complexity trade-off
- Reduction with bounded discrepancy



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Robust Verification for Linear Systems: Example



System:

$$\dot{x}(t) = A_i x(t) + b_i U_{in}(t)$$

$$U_{out}(t) = Cx(t)$$

Step input ($t > 0$):

$$U_{in}(t) = 1$$

Steady state at $t = 0$:

$$x(0) = -A^{-1}bU_{in}(0)$$

Property:

$$\Phi = G \pi_1 \wedge F_{[0,0.85]} G \pi_2$$

$$O(\pi_1) = [-1.5, 1.5]$$

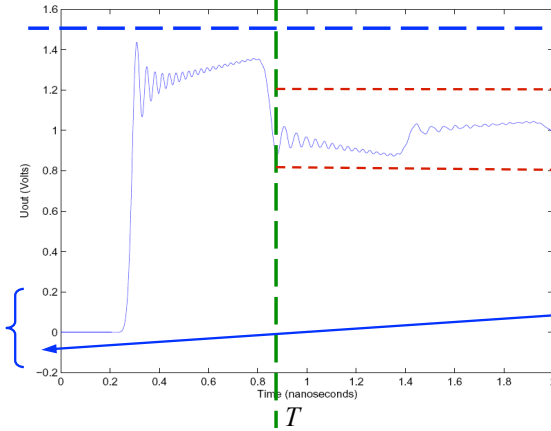
$$O(\pi_2) = [0.8, 1.2]$$

Initial conditions:

$$U_{in}(0) \in [-0.2, 0.2]$$

Uncertain parameters

$$e.g. C \in [a_1, a_2]$$



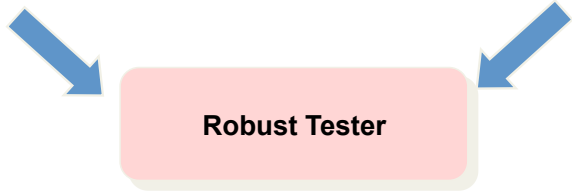
This is a transmission line system. A ~80 dimension linear system. The property we want to verify is that the output $y(t)$ globally stays within Π_1 $(-1.5, 1.5)$, and $y(t)$ enters Π_2 $(0.8, 1.2)$ within $[0, 0.85]$ time interval. Such kind of properties are closely related to common control performance metrics like rise time, settling time, constraints on input/state, etc. This shows the properties we are interested in and how to interpret the properties

Problem Formulation

Given a closed-loop system model, and a set of specifications, we want a tester to tell whether the system satisfies the specifications, in the sense that the set of all possible system traces is a subset of all traces on which the specifications are true

Closed-loop system Σ
 $\dot{x} = f(x; p; u)$
 $y = g(x; p; u)$
 $X_0 \subseteq X$

Specification Φ

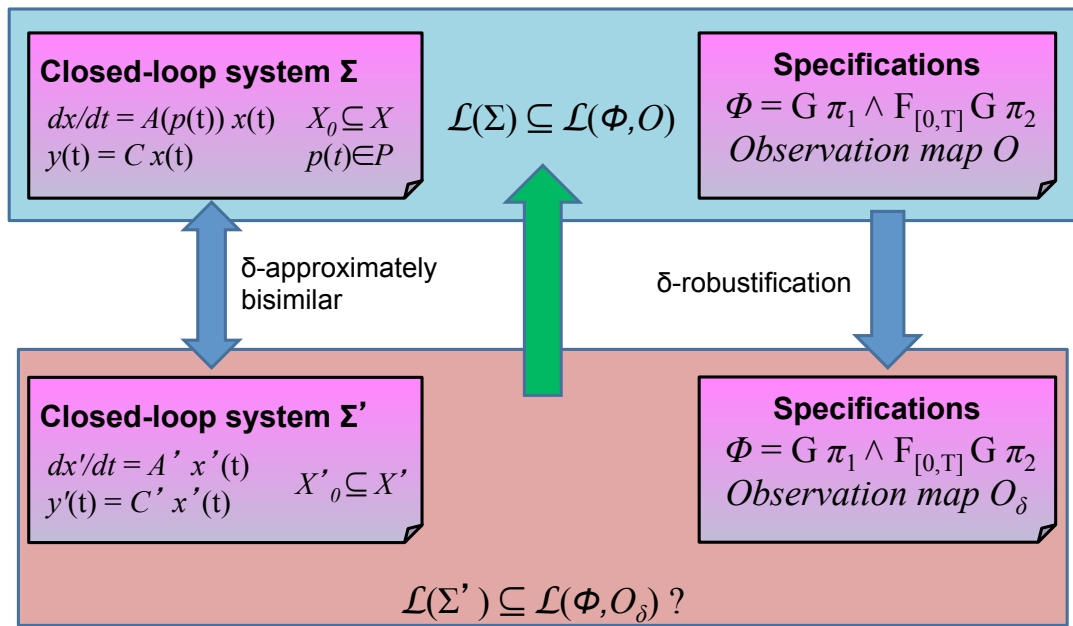


$L(\Sigma) \subseteq L(\Phi)$



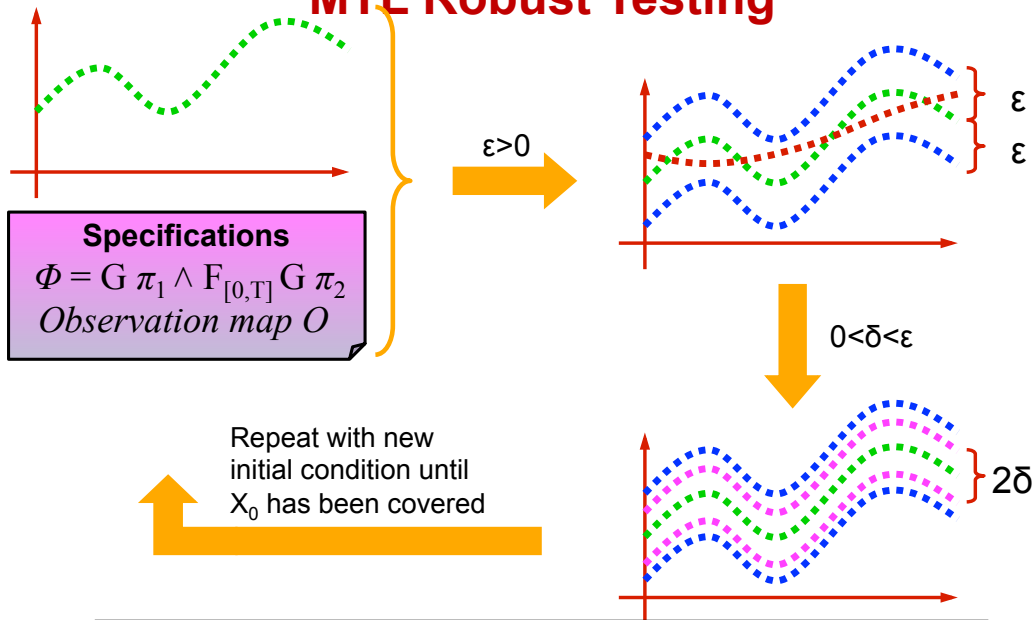
Fainekos, Girard and Pappas, *Temporal logic verification using simulation*, FORMATS 2006
 Julius, Fainekos, Anand, Lee, Pappas, *Robust Test Generation and Coverage for Hybrid Systems*, HSCC 2007
 Fainekos, Pappas, *MTL Robust Testing and Verification for LPV Systems*, ACC 2009

Solution Overview



The key idea of our solution is: Given the original closed-loop system, where the matrix A depends on some time-varying uncertain parameters $p(t)$, we first try to find a fixed linear system A' that is a close approximation of the original system, in the sense that the output traces of the original system always (despite uncertain $p(t)$'s) stay within Δ distance to the traces of the reduced system. Then if we can show that the specifications are satisfied by the reduced system with some robustness constraints (explained in the next slide), then we can infer that the original system also satisfy the properties

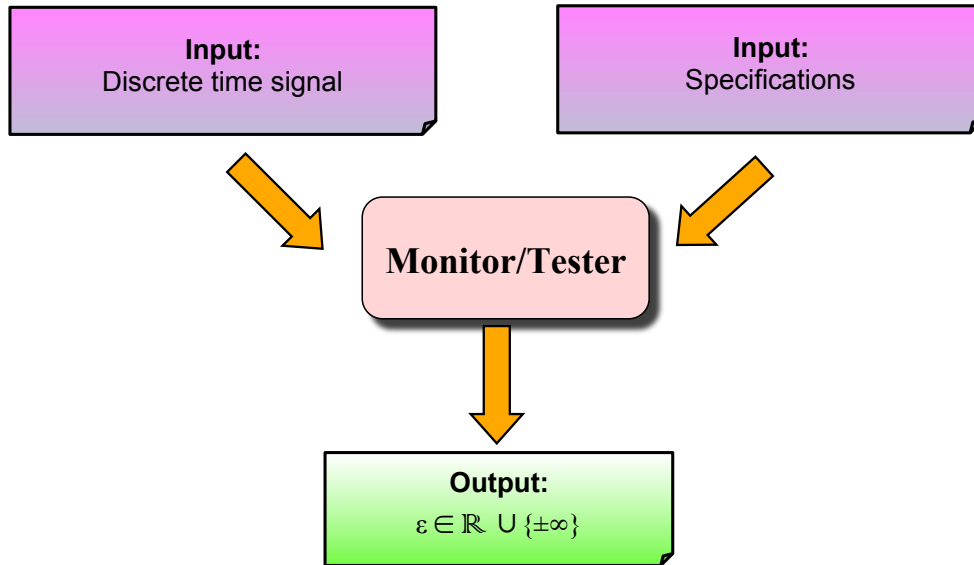
MTL Robust Testing



Fainekos, Girard and Pappas, *Temporal logic verification using simulation*, FORMATS 2006

This slide illustrate intuitively how the approach works: Given a system trace of the reduced system and the specifications, we have a software tool (next slide) to calculate a robustness bound ϵ , meaning that the specification is locally satisfied anywhere within the ϵ -"tube" (the region between to blue lines) around the given trace. Next if we can show that the "difference" between the reduced system and the original system is always within the "tube", then it is inferred that the original system traces also satisfy the specifications

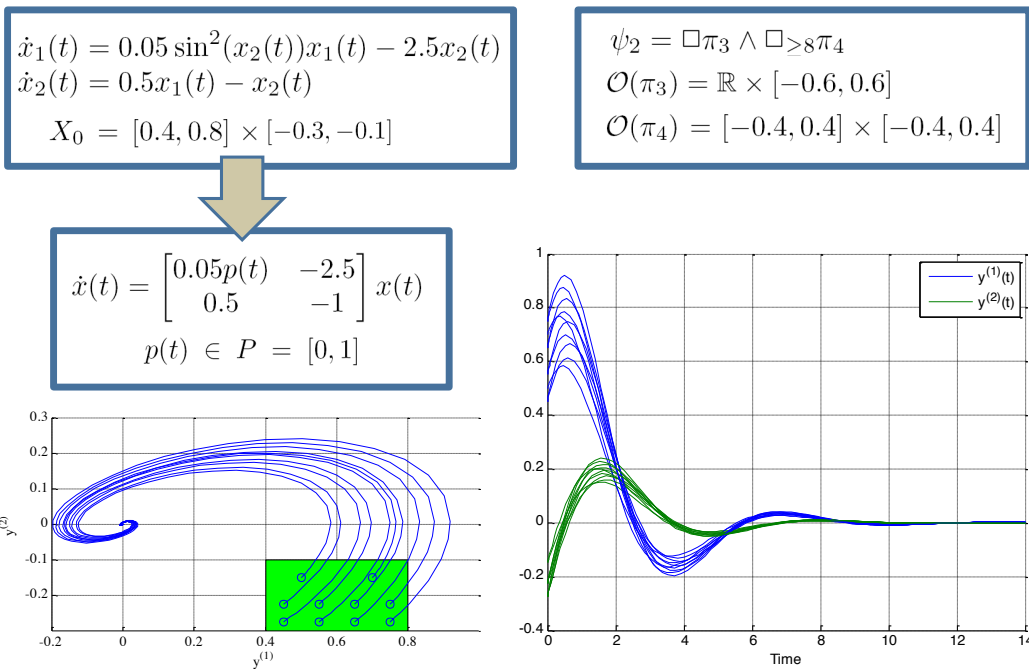
Software toolbox : TaLiRo



Available at : <http://www.seas.upenn.edu/~fainekos/robustness.html>

We have a software tool such that given a system trace and specifications, the tool calculate the robustness bound epsilon, meaning that the specifications are satisfied within a epsilon-tube around the given trace

Example : Nonlinear systems



Here is an example of extending the approach to simple non-linear systems: In the model, the only non-linear term is $\sin^2(x_2)$, rather than dealing with the non-linear system, we transform the system into a linear system with uncertain parameters, by replacing $\sin^2(x_2)$ with a parameter P , which is unknown but bounded (within $[0,1]$). Next, if we can show that all possible traces of the linear system (with uncertain P) satisfy the specifications, we know the original system also satisfy the same specifications.

Adaptive/Robust Extension

- Possible to extend the robust verification results on linear systems to large non-linear systems
 - Partition parameter space into several regions
 - Example: highly insulin-sensitive, average, and insulin-resistant subjects

Insulin Sensitivity Coefficient: within [3,10]		
Insulin resistant	Average	Insulin sensitive
[3,5]	[5,8]	[8,10]

- Robustness verification within each region
- Adaptive exploration to determine which region a newly admitted subject belongs to
 - Exploration phase must satisfy safety properties

Safety Analysis

- Identify platform hazards in the networked control setting
 - Develop mitigation strategies
 - Unlike the closed-loop PCA system, where only overdosing is undesirable, in the BG system, both hypo- and hyper-glycaemia need to be avoided
 - No trivial fail-safe mode for closed-loop BG control
 - System-level safety verification and validation to show that patient safety is guaranteed in the networked system, even under failure conditions